

CSSE 220

Day 21

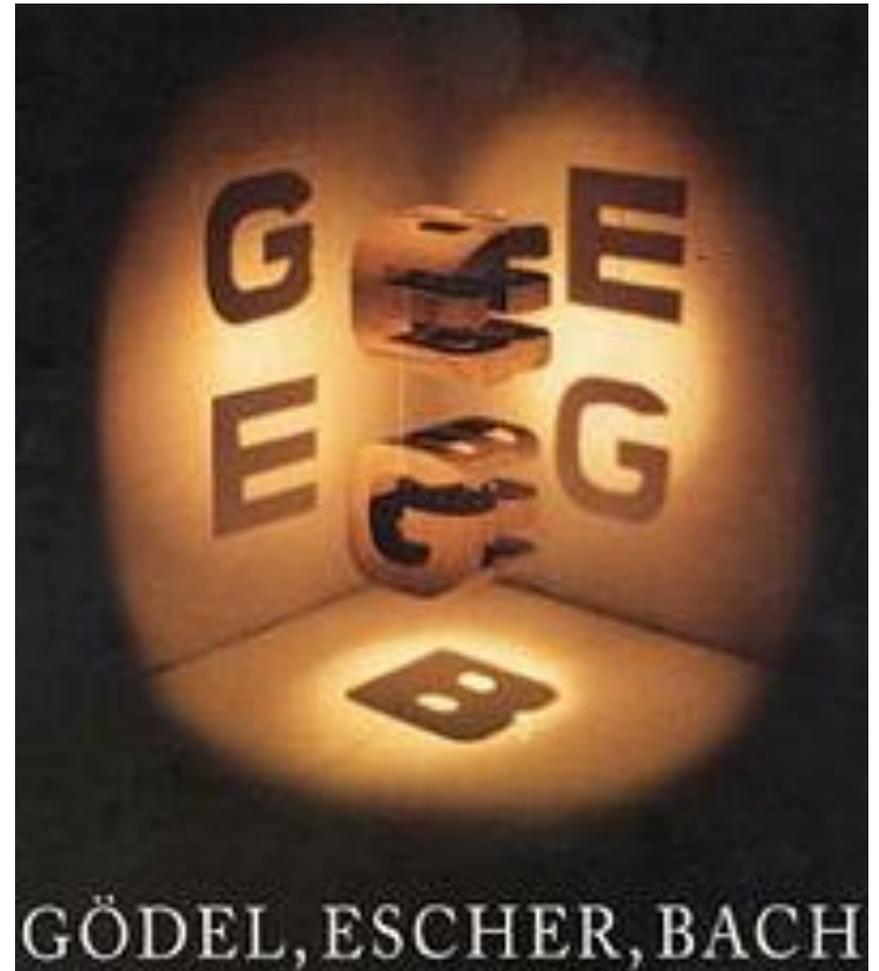
Recursion

Checkout *Recursion* project from SVN

Questions?

Gödel, Escher, Bach

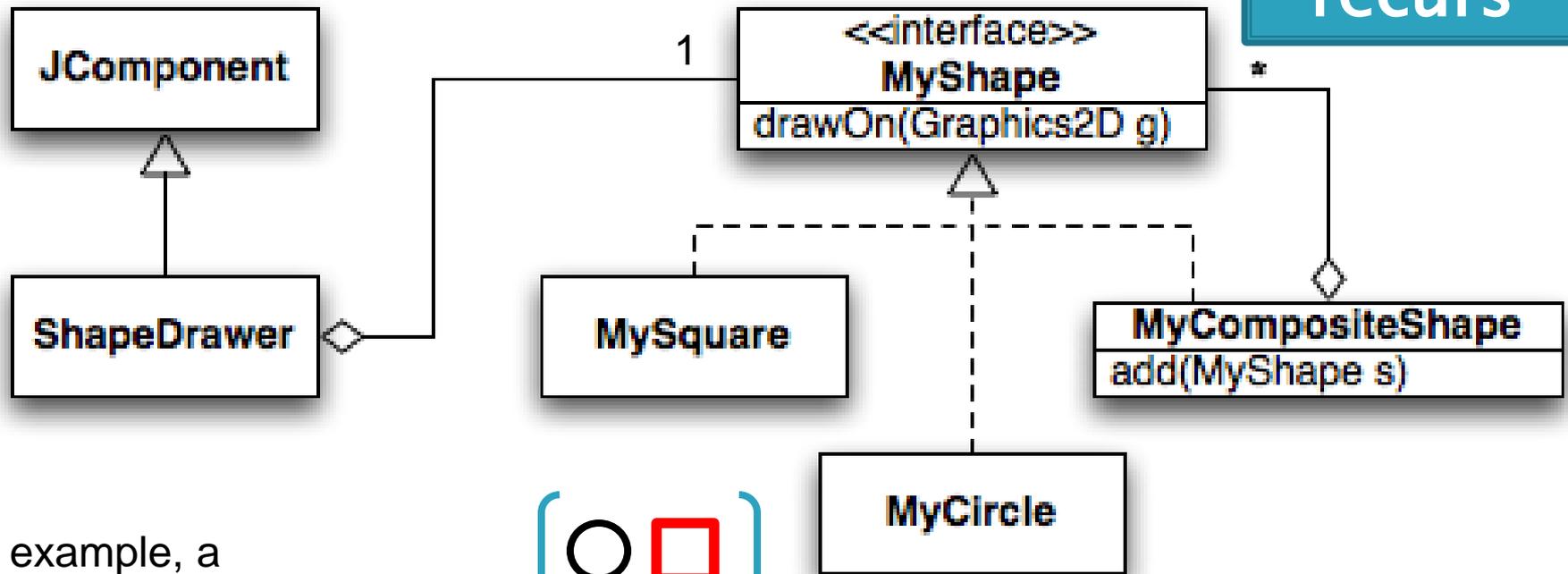
- ▶ By Douglas Hofstadter
- ▶ Argues that intelligence arises (in part) because of **our ability to think about thinking**



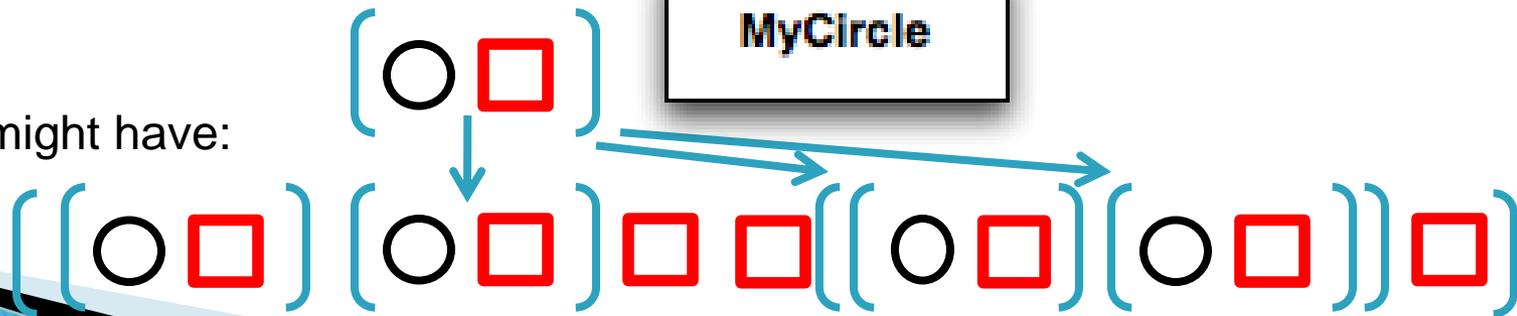
Recursion

- ▶ A solution technique where the same computation occurs repeatedly as the problem is solved

recurs



For example, a ShapeDrawer might have:



An example – Triangle Numbers

- ▶ If each red block has area 1, what is the *area* $A(n)$ of the Triangle whose *width* is n ?

- Answer:

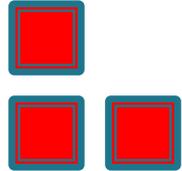
$$A(n) = n + A(n-1)$$

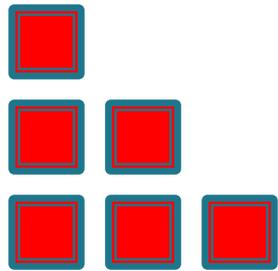
- ▶ The above holds for what n ? What is the answer for other n ?

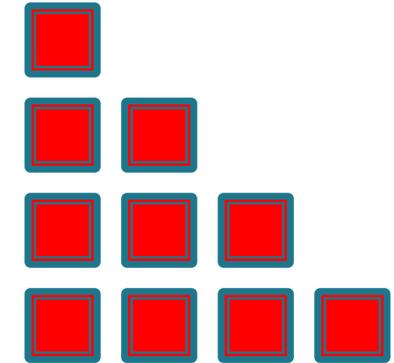
- Answer: The recursive equation holds for $n > 1$.

For $n = 1$, the area is 1.

Triangle with width 1 {  }

Triangle with width 2 {  }

Triangle with width 3 {  }

Triangle with width 4 {  }

Q1

Let's see how this translates naturally to code.
Then let's trace the execution of the code (next slide).

Frames for Tracing Recursive Code

1. Draw box when method starts

2. Fill in name and first line no.

3. Write class name (for static method) or draw reference to object (for non-static method)

method name, line number

scope box

parameters
and local variables

4. List every parameter and its argument value.

5. List every local variable declared in the method, **but no values yet**

6. Step through the method, update the line number and variable values, draw new frame for new calls

7. "Erase" the frame when the method is done.

Thanks for
David Gries for
this technique

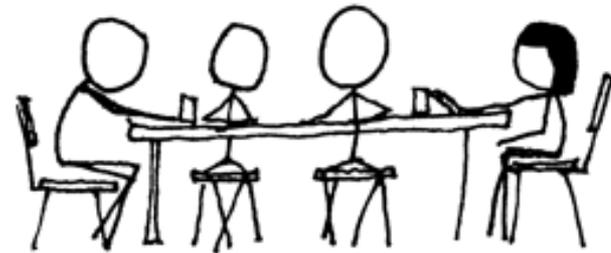
Q2-9

Tabletop Roleplaying

I may have also tossed one of a pair of teleportation rings into the ocean with interesting results.

YOUR PARTY ENTERS THE TAVERN.
I GATHER EVERYONE AROUND A TABLE. I HAVE THE ELVES START WHITTLING DICE AND GET OUT SOME PARCHMENT FOR CHARACTER SHEETS.

HEY, NO RECURSING.



Key Rules to Using Recursion

- ▶ Always have a **base case** that **doesn't recurse**
- ▶ Make sure recursive case always makes **progress**, by **solving a smaller problem**
- ▶ **You gotta believe**
 - Trust in the recursive solution
 - Just consider one step at a time

Programming | Problem

- ▶ Add a *recursive* method to Sentence for computing whether Sentence is a palindrome

- A *palindrome* is a String that is the same backwards as forwards
 - We will ignore punctuation, spaces, and case.
- **Key idea: use the definition of *isPalindrome()* in defining *isPalindrome()* . How can we make progress to a smaller problem?**

- Here,

`x.isPalindrome()` iff `____.isPalindrome()` _____ ?

- `x.isPalindrome()` iff `xMinusFirstAndLastLetter.isPalindrome()` and _____ ?

`x.isPalindrome()` iff `xMinusFirstAndLastLetter.isPalindrome()`
and first letter equals last letter

Examples of palindromes from

http://www.fun-with-words.com/palin_example.html

Never odd or even

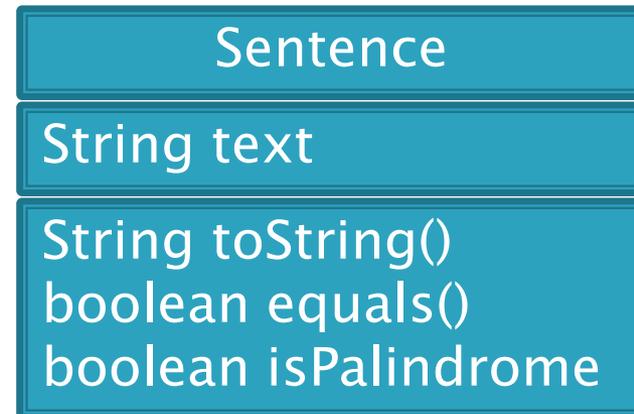
Murder for a jar of red rum

May a moody baby doom a yam?

Go hang a salami; I'm a lasagna hog!

Oozy rat in a sanitary zoo

Do geese see God?



Don't worry about punctuation, spaces and case at this point of your thinking.

Recursive Helpers

- ▶ Our `isPalindrome()` makes lots of new Sentence objects
- ▶ We can make it better with a “recursive helper method”
 - ▶ Many recursive problems require a helper method

```
public boolean isPalindrome() {  
    return isPalindrome(0, this.text.length() - 1);  
}
```



Position of first letter of the remaining String to check



Position of last letter of the remaining String to check

Homework part 1

- ▶ Reverse a string...recursively!
- ▶ A recursive helper can make this really short!

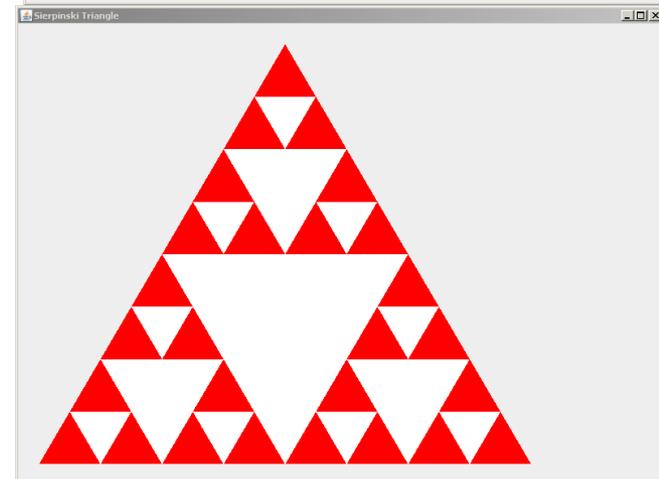
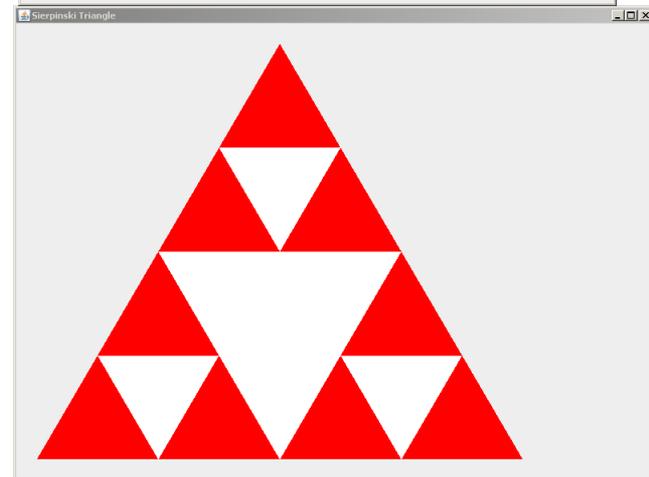
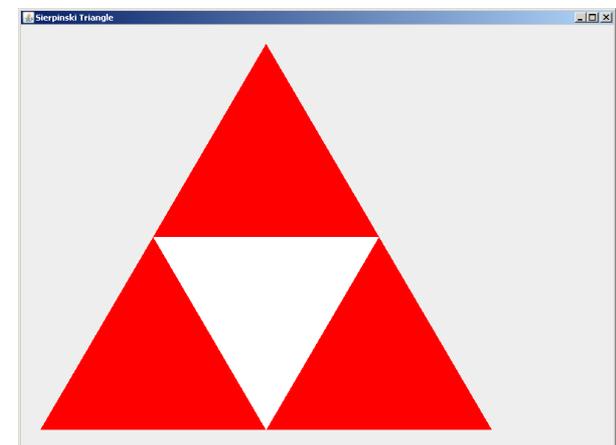
Another Definition of Recursion

- ▶ “If you already know what recursion is, just remember the answer. Otherwise, find someone who is standing closer to Douglas Hofstadter than you are; then ask him or her what recursion is.”

—Andrew Plotkin

HW, part 2: Sierpinski

```
private void drawSierpinski(Graphics2D g,  
    double left, double bottom,  
    double base) {  
    // TODO Don't forget your base case  
  
    // Draws the first equilateral triangle  
    // called for by the algorithm.  
    Point2D p1 = new Point2D.Double(  
        left, bottom);  
    Point2D p2 = new Point2D.Double(  
        left + base, bottom);  
    Point2D p3 = new Point2D.Double(  
        left + base / 2.0,  
        bottom - base * HEIGHT_TO_BASE_RATIO);  
    Shape triangle = makeTriangle(  
        p1, p2, p3);  
  
    g.setColor(Color.RED);  
    g.fill(triangle);  
  
    // TODO Implement rest of this method.  
}
```



Recursive Functions

- ▶ Factorial:

$$n! = \begin{cases} 1 & \text{if } n \leq 1 \\ n * (n - 1)! & \text{otherwise} \end{cases}$$

Base Case

Recursive step

- ▶ Ackermann function:

$$A(m, n) = \begin{cases} n + 1 & \text{if } m = 0 \\ A(m - 1, 1) & \text{if } m > 0 \text{ and } n = 0 \\ A(m - 1, A(m, n - 1)) & \text{otherwise} \end{cases}$$

Exam 2 is next Friday morning. Major topics are:

- UML class diagrams and how to implement them
- event-driven programming
- GUI programming
- polymorphism
- interfaces
- inheritance
- recursion

Work Time

Work on VectorGraphics with your team

- Cycle 1 code and status report and Cycle 2 user stories are due Tuesday.
- Or work on recursion problems, due Thursday